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# Implications of Giaquinto's epistemology of visual thinking to the teaching and learning of fractions

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# Summary

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- 1) My research
- 2) Giaquinto's ideas
- 3) Reasoning
- 4) Implications

# My research goal

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**Goal:** Investigate how do low achieving students learn fractions through an approach emphasizing visual representations.

**Motivation:** Evidences that visual representations could be particularly beneficial for low achieving students (Gates, 2015; Barichello, 2015)

# My data collection

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- I observed lessons for low achieving students in one British secondary school;
- Designed 12 lessons\* about fractions
  - emphasizing visual representation; and
  - Coherent with school practices;
- Observed 3 teachers enacting the lessons with 1 low achieving group each;
- Collected worksheets and within-class clinical interviews.

\* <http://www.barichello.coffee/about-my-research/lessons-fractions-visual-representations>

# My initial impressions

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- Students being able to answer “why” questions;
- Students using vocabulary related to visual representations;
- Students being able to extend their knowledge to solve generative questions (Barichello, 2015);
- Teachers noticing that the learning was somehow different.

# Summary

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1) My research and this presentation

»» 2) Giaquinto's ideas

3) Reasoning

4) Implications

# Giaquinto's ideas

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**Book:** Visual thinking in mathematics: an epistemological study (Giaquinto, 2007)

**Article:** Visualizing as means of geometrical discovery (Giaquinto, 1992)

**Main points:** Visualization can form basic geometrical concepts and can trigger new knowledge.

# What is visualization?

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**Visualization:** mental ability to notice certain properties of and operate on visual representations.

It is:

- Partially innate;
- Partially developed by seeing;
- Partially developed by learning where to focus attention.

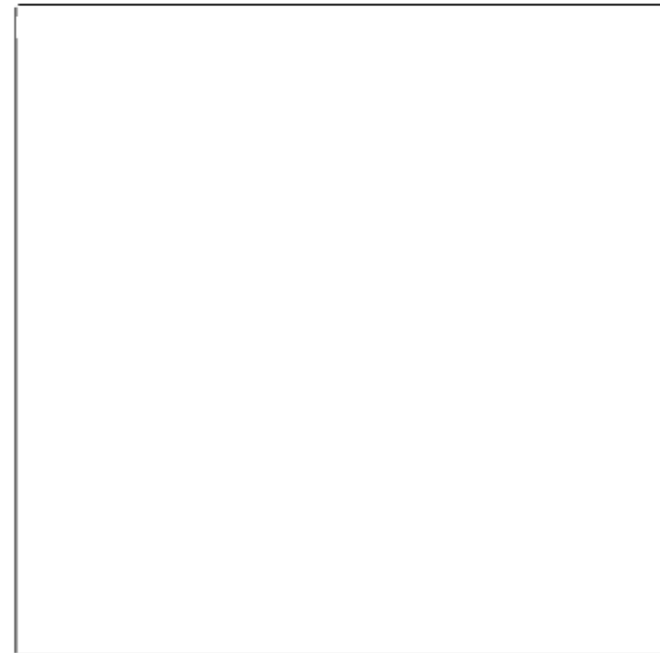


# Giaquinto's main ideas

1) A visual experience can be a constituent of a thought, then lead to concept formation.

Example: *Uncle is a brother of my father or mother.*

2) By applying visual transformations on visual concepts, we can acquire new knowledge.



Square A

# Giaquinto's ideas - some remarks

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- "Sense experience does enter into the causal prehistory of the belief, not as evidence but as raw material from which the mind forms our geometrical concepts" (Giaquinto, 2007)
- It is not the only way of getting to know something;
- It is not automatic, it demands intention;
- It is not only for geometrical concepts;

# Summary

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»» **3) Reasoning**

**4) Implications**

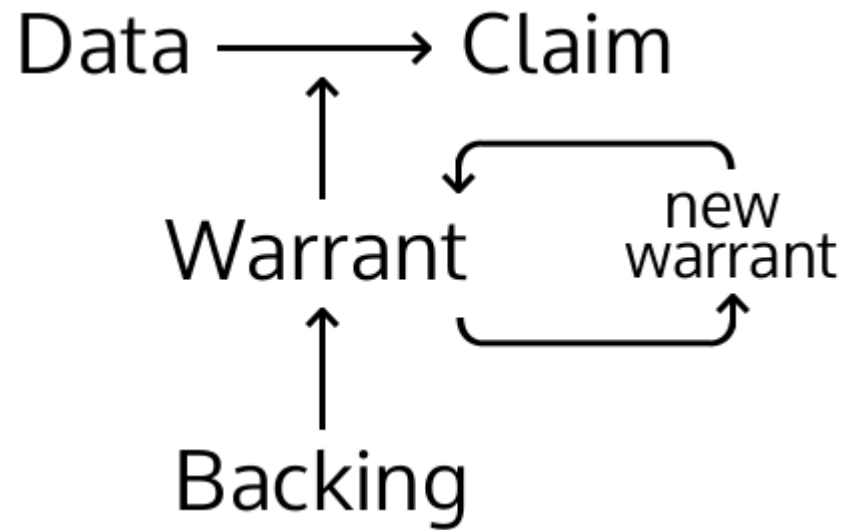
# What is reasoning?

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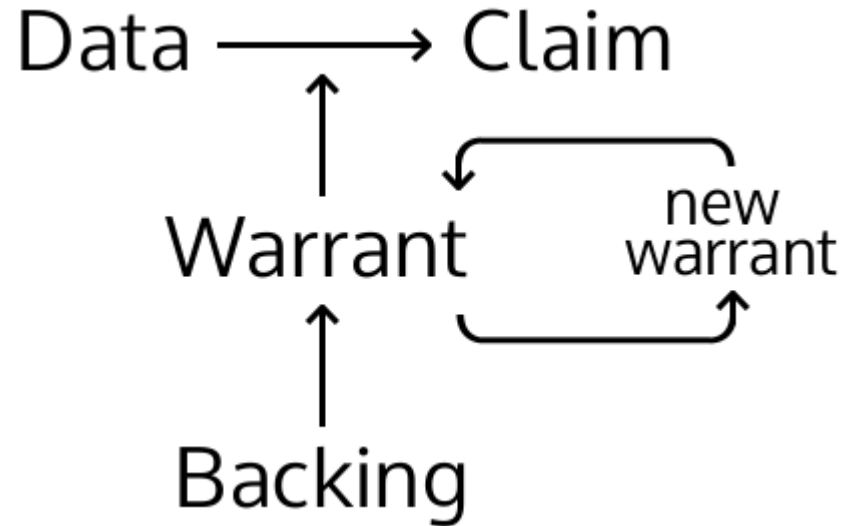
**Reasoning:** sequence of arguments that supports the solution of a task.

**Manifestation:** students answering to “why” and “how” questions.

# Toulmin's layout of an argument

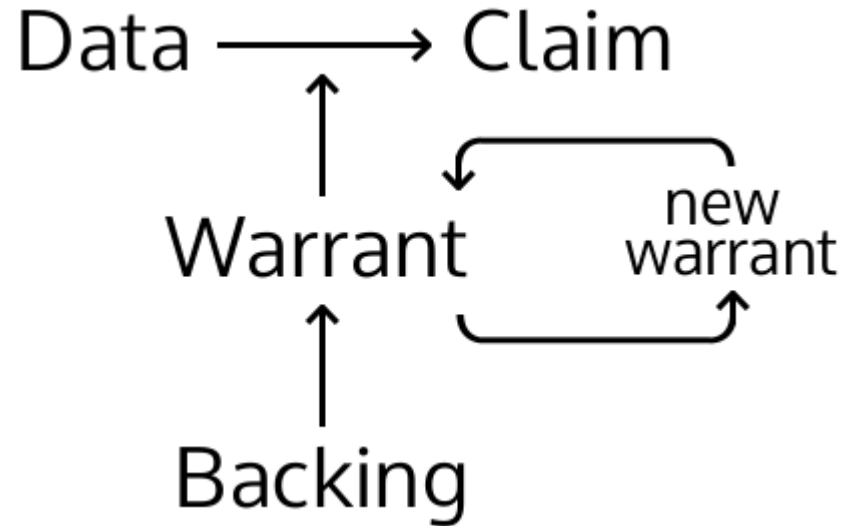


# What kind of warrants are there?



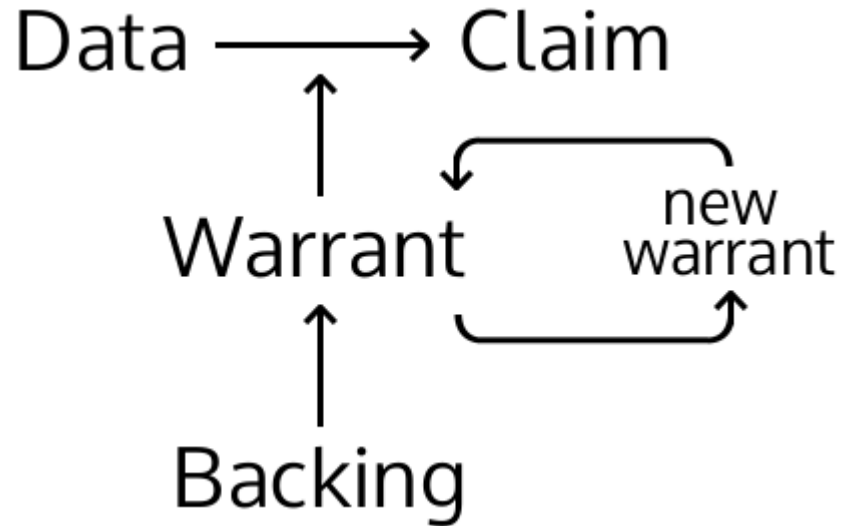
**1<sup>st</sup> possibility: Authority**

# What kind of warrants are there?



**2<sup>nd</sup> possibility: Algorithm**

# What kind of warrants are there?



**3<sup>rd</sup> possibility:** Prior knowledge (mathematical)



# What kind of warrants are there?

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4<sup>th</sup> **possibility**: visualization

“visualizing can constitute a warrant for mathematical belief” (Rodd, 2000)

# Summary

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# Implications

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Remember that visualization is:

- Partially innate;
- Partially developed by seeing;
- Partially developed by learning where to focus attention.

# Implications

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Therefore:

- Teachers should focus on a small number of powerful models;
- Teachers have to teach the orthography and grammar of a model;
- Teachers have to recognize the validity of visual arguments;

# Thank you!

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# Bibliography

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